

## MODEL TREES WITH TOPIC MODEL PREPROCESSING: AN APPROACH FOR DATA JOURNALISM ILLUSTRATED WITH THE WIKILEAKS AFGHANISTAN WAR LOGS

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The WikiLeaks Afghanistan war logs contain nearly 77,000 reports of incidents in the US-led Afghanistan war, covering the period from January 2004 to December 2009. The recent growth of data on complex social systems and the potential to derive stories from them has shifted the focus of journalistic and scientific attention increasingly toward data-driven journalism and computational social science. In this paper we advocate the usage of modern statistical methods for problems of data journalism and beyond, which may help journalistic and scientific work and lead to additional insight. Using the WikiLeaks Afghanistan war logs for illustration, we present an approach that builds intelligible statistical models for interpretable segments in the data, in this case to explore the fatality rates associated with different circumstances in the Afghanistan war. Our approach combines preprocessing by Latent Dirichlet Allocation (LDA) with model trees. LDA is used to process the natural language information contained in each report summary by estimating latent topics and assigning each report to one of them. Together with other variables these topic assignments serve as splitting variables for finding segments in the data to which local statistical models for the reported number of fatalities are fitted. Segmentation and fitting is carried out with recursive partitioning of negative binomial distributions. We identify segments with different fatality rates that correspond to a small number of topics and other variables as well as their interactions. Furthermore, we carve out the similarities between segments and connect them to stories that have been covered in the media. This gives an unprecedented description of the war in Afghanistan and serves as an example of how data journalism, computational social science and other areas with interest in database data can benefit from modern statistical techniques.

**1. Introduction.** Analyses of fatalities in wars and armed conflicts are an eminent subject of systematic investigation. Most of them have been conducted in

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a historical context, often retrospectively estimating the number of and circumstances under which fatalities of war occurred. There are literally hundreds of historical investigations into numerous wars; see, for example, [Garfield and Neugut \(1991\)](#) for a review of the last 200 years.

Notwithstanding such efforts, contemporary systematic scientific investigation into the number of fatalities in wars are relatively rare and more closely tied to the emergence of statistics and epidemiology as disciplines rather than to the discipline of history. Some of the first examples we could find were [Marshall and Balfour \(1838\)](#) or [Nightingale \(1863\)](#). While these investigations were still firmly rooted in descriptive statistics, statistical modeling was about to become imperative as [Bortkiewicz \(1898\)](#) published his seminal work on the use of the Poisson distribution for rare events which he motivated by the analysis of deaths of Prussian soldiers by horse kicks. To our knowledge, this was the first instance of a parametric and inferential approach to analyze fatalities of war. Contemporary investigations into the number and circumstances of casualties of war that made use of statistical modeling next to descriptive approaches have increased since then, for example, [Spiegel and Salama \(2001\)](#), [Thomas et al. \(2001\)](#), [Lakstein and Blumenfeld \(2005\)](#) or [Holcomb et al. \(2007\)](#).

In the last decade their number seems to peak<sup>2</sup> arguably because data on war fatalities are much easier to come by. Recent work, for example, for the war in Afghanistan, includes the studies on child casualties by [Bhutta \(2002\)](#) and on military fatalities by [Bird and Fairweather \(2007\)](#) or [Bohannon \(2011\)](#). Other recent work in this field has been done by [Burnham et al. \(2006\)](#), [Buzzell and Preston \(2007\)](#), [Degomme and Guha-Sapir \(2010\)](#), [Haushofer, Biletzki and Kanwisher \(2010\)](#).

In July 2010 the availability of data on a specific war became unprecedented, as whistleblower website WikiLeaks released a massive amount of military classified war logs from the Afghanistan war into the public. These documents constitute a “war diary” of the military operation in Afghanistan, containing a detailed description of what happened in each event for which a report was filed, including counts of killed and wounded people, local and administrative information, temporal and spatial information and a short written description of each particular incident. The documents themselves stem from a database of the US army and, along the lines of WikiLeaks, they do not generally cover any top secret operations or European or other operations of the International Security Assistance Force (ISAF). In total, the war logs consist of 76,911 documents and cover the time period between January 2004 and December 2009. They provide an unprecedented view of the war in Afghanistan with an information abundance that has previously been unknown and has only been topped by the release of the Iraq war logs some months later.

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<sup>2</sup>According to a quick survey in the ISI Web of Knowledge citation database, searching for “war casualties” in March 2011 found 1476 records, 840 of which were published after 2000. 580 of those were published no earlier than 2005.

Interestingly, the scientific community has been rather hesitant in approaching the data [but see Conway (2010), O’Loughlin et al. (2010), Zammit-Mangion et al. (2012) for notable exceptions]. In journalism and the media world, however, the impact of the release was very strong. The German news magazine *Der Spiegel* wrote that the editors-in-chief of *Der Spiegel*, *The New York Times* and *The Guardian* were “unanimous in their belief that there is a justified public interest in the material” [Gebauer (2010)] and the war diary was marked as the 21st century equivalent of the Pentagon Papers from the 1970s. However, while the Pentagon Papers have provided an aggregated view on the war in Vietnam, the WikiLeaks war diary is an account of the daily events in Afghanistan containing thousands of mosaic tiles describing incidents from the perspective of the US forces. They were written by different people and are sometimes accurate and sometimes possibly not. The war logs themselves neither contain information on strategic decisions nor do they provide a coherent, general picture of the war. Hence, each media outlet had to write its own stories based on the material [see O’Loughlin et al. (2010)]. This take on the WikiLeaks Afghanistan war logs has been praised as data-driven journalism in action [see Rogers (2010)].

To elicit stories out of complex data is a contemporary issue for journalists and (social) scientists, especially when the amount of data is large and cannot be processed easily by humans. This is where data journalism or database journalism (a type of journalism which allows stories to unfold from data) and computational social science [the science that investigates social phenomena through advanced information processing technologies, e.g., Cioffi-Revilla (2010)] come into play. Data journalism and computational social science both use statistical and computational methods to deal with the problem of processing large and complex data (often in the form of text documents) and presenting them in an accessible form. For example, a popular approach is to narrow down the data by keyword searches with the goal to find a relevant subset that can be processed by a human reader. Another one is to count the frequency of words within documents to allow for a broad overview of the data or to extract additional information that can be used for telling a story without the need for directly reading or processing all data points [see, e.g., Cohen, Hamilton and Turner (2011), Hofmarcher, Theußl and Hornik (2011)]. More advanced approaches may aim at clustering the documents into “similar” sets of documents, for example, via bag of words models [see Zhang, Jin and Zhou (2010)]. This allows the journalist or scientist to find the story by reading just a few documents within each cluster. Another approach might be to derive structure from unstructured data by, for example, using network analysis [e.g., Lazer et al. (2009)] and similar methods. Often a description or a visualization is the primary goal of such procedures, but in principle the analysis is not limited to that.

Regarding the WikiLeaks Afghanistan war logs, analyses up to the point of writing this paper have remained mostly on a descriptive level and if insights from an inferential or modeling approach have been gained, it was mostly by using a

small amount of the information available. This could be due to the nature and bulk of the data. One of the peculiarities of the war log and its main challenge is that the data at hand stem from a database and that the information is captured in both numeric variables as well as written text. To neglect the written text in a statistical evaluation of such data sets would often come along with discarding important, if not crucial, information. Especially in the WikiLeaks data, nearly all detailed information about the events is stored as written text. Thus, it is essential for a deep statistical probing to incorporate that information.

Modern statistical procedures provide tools to handle, analyze and model such data sets appropriately and therefore allow a more thorough investigation. In this paper we will make exemplary use of statistical learning procedures to segment the reports in the war logs and to build local statistical models for the number of fatalities in each segment. By combining two modern ideas, topic models and model-based recursive partitioning, our analysis allows to draw a bigger picture of the war from the thousands of mosaic tiles. In doing so, we present an approach that might be particularly suitable for, but not limited to, data journalism and social science, especially since in the end it provides palpable segments of data points characterized by a small number of parameters that directly relate to the question at hand.

The idea of our approach is as follows: each single entry in the WikiLeaks war logs contains several variables and also a written report summary containing a short description of what happened in the particular incident. We are interested in extracting explanatory information from the reports, some type of meta information that aggregates reports with similar content. We achieve this by using Latent Dirichlet Allocation [LDA; Blei, Jordan and Ng (2003)] which clusters written report summaries into latent topics. In a second step, we then use the generated topic assignments as variables from which we infer a segmentation of the reports and locally model the number of fatalities in each segment. The provided fatality counts function as our target variable. Since there is a high degree of overdispersion present, we use a negative binomial distribution [Lawless (1987)] model in each segment. This enables to estimate the distribution of deaths per segment appropriately. To allow for a flexible, nonlinear, interaction-focused functional relationship between splitting variables and the local model, we employ the model-based recursive partitioning framework of Zeileis, Hothorn and Hornik (2008).

The remainder of this paper is organized as follows: Section 2 contains a description of the WikiLeaks war logs. The methodological Section 3 presents the methods used. The results are described and discussed in Section 4. In Section 5 we provide validation of the results. We finish with conclusions in Section 6. This paper is accompanied by supplementary material [Rusch et al. (2013a, 2013b)].

**2. The WikiLeaks Afghanistan war logs.** The release of 76,911 individual war logs by [WikiLeaks.org](http://WikiLeaks.org) provides an unprecedented possibility to take a look at an ongoing war. The war logs cover the period from January 2004 to December

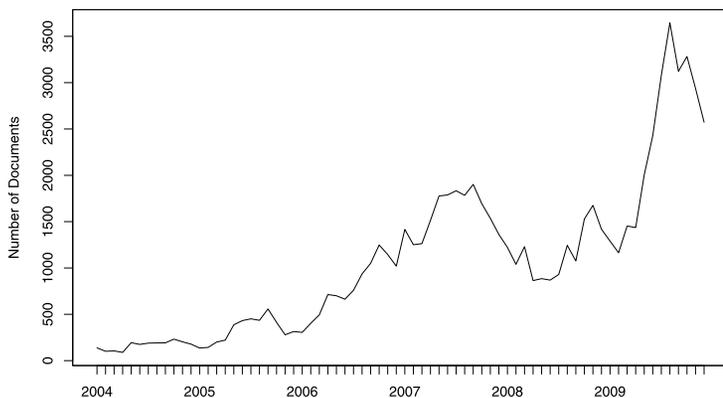


FIG. 1. *Monthly quantity of filed reports.*

2009 and each event for which a report has been filed corresponds to a single document. Figure 1 displays the number of filed reports per month. While for the first years of the military operation we can find only a few hundred reports per month, this number increases up to more than 3500 per month in mid 2009.

Each report contains 32 numerical and factor variables. They include four variables listing the number of “Civilian,” “Enemy,” “Friend” and “Host” fatalities within each report. The sum of these fatalities for each report serves as our target variable. Note that fighters opposing coalition troops are referred to as “Enemies.” We adopt the term “Anti Coalition Fighters” (ACF) to denote this variable. The “Friends” column refers to ISAF forces including the NATO countries and the US military, while “Host” stands for local (Afghan) military and police. We subsume the former under “coalition troops” or “allied forces” and the latter under “Afghan or host forces.”

Table 1 provides summary statistics of the reported casualties and Figure 2 displays a plot of the number of fatalities over time for each group during the observation period. In total we find 24,155 fatalities in the war logs. 63% of the fatalities are labeled as ACF. The second highest fatality number (16.54%) is observed for civilians, closely followed by 15.72% Afghan soldiers and policemen and 1146 or 4.74% killed allied soldiers. Palpable are the two peaks for killed insurgents in late summer 2006 and 2007 in Figure 2. They account for 943 killed ACF fighters dur-

TABLE 1  
*The number of casualties by group*

|         | Allied | Host | Civilian | ACF    | Total  |
|---------|--------|------|----------|--------|--------|
| Killed  | 1146   | 3796 | 3994     | 15,219 | 24,155 |
| Wounded | 7296   | 8503 | 9044     | 1824   | 26,667 |

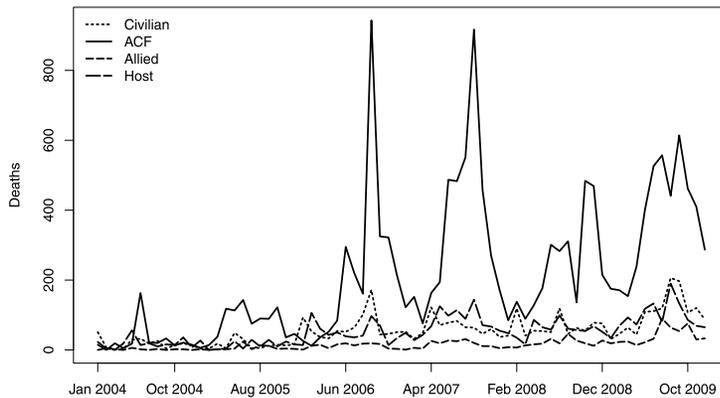


FIG. 2. *Monthly counts of fatalities by group.*

ing September 2006 and for 917 in September 2007. The former peak corresponds to “Operation Medusa,” an operation that had the aim to establish government control over areas of the Kandahar province. The latter marks operations near Kandahar in an effort to remove insurgents who had returned to this area. Mid to late 2009 is the bloodiest period for civilians, coalition soldiers and ACF in the data. Between May 2009 and December 2009 we observe 1056 (26.4%) out of 3994 civilian fatalities (see Table 1). In August 2009, during the period of the Afghan presidential election (August 20), we observe 206 civilian victims and 190 killed ACF. For both groups, this is the highest death toll within one month. Roughly the same situation is observed for allied soldiers. Here the monthly maximum of 90 deaths happens in July 2009 and from May 2009 to December 2009 the data account for 346 (30.2%) killed allied soldiers.

In addition to the fatality numbers, the reports contain 28 numerical and factor variables that serve as split candidate variables for the segmentation. We restrict ourselves to describing only those splitting variables that have a special relevance for our analysis.

The factor `attackOn`, with its levels `FRIEND`, `NEUTRAL`, `ENEMY`, `UNKNOWN` encodes the US military’s point of view on whom an “attack” (action) is directed during the incident. O’Loughlin et al. [(2010), page 474, ff] state that this variable seems to have been mislabeled and should have been named “`attackBy`.” However, after inspection of a random sample of about 100 report summaries of the war logs, we believe that `attackOn` does not contain information about who carried out a certain action but rather contains information about on whom the action described in the report is directed. For instance, leaflets of Anti Coalition Forces (ACF) calling for attacks against the US forces are categorized as `attackOn=NEUTRAL`, fire fights between ACF and allied soldiers as `attackOn=ENEMY` and friendly fire is labeled as `attackOn=FRIEND`.

The categorical variable `color` controls the display color of the message in the messaging system and map views. Messages relating to enemy activity have

the color red, those relating to friendly activity have been colored blue, and green stands for neutral. This variable can be seen as the one encoding by whom an action has been carried out (i.e., “attackBy”).

Another important variable for our analysis is `region`, roughly describing where an event took place. It has levels RC NORTH, RC EAST, RC WEST, RC SOUTH, RC CAPITAL, UNKNOWN and NONE SELECTED (RC stands for “Regional Command”).

Last, there is `complexAttack`, a categorical variable with levels TRUE, FALSE and NA (not available) that encodes the complexity of an attack. The US military states an attack as complex if it has been well organized and executed, if soldiers have made use of heavy artillery and the troops have been able to withdraw from the battlefield in an organized fashion [see [Roggio \(2009\)](#)].

*The report summaries.* The variables described above, which may serve as split candidate variables for segmenting the data set, only allow for a rather limited view into the events associated with each report and therefore the circumstances under which fatalities have happened. We can, however, find additional information about the context of the various incidents in the provided report summaries, which contain a short verbal description of what transpired during the incident. To give an example, for 19-Jul-2005 we can find the following report:

On 19 July, at about 0730 hrs, a BBIED went off on an alleged suicide bomber targeting Enjeel district Chief of Police. As a result, the attacker was instantly killed, but no injuries to anyone else was reported. Police investigation is ongoing.

The report summaries tell us the hows and whys of the mission in a very detailed way, something the other provided variables cannot. Thus, the report summaries and their content are at the core of evaluating the ongoings of this war as portrayed in the war logs as well as gaining insight into mortality in different situations. Disregarding these summaries in evaluating the war logs would be equivalent to discarding the most important information for describing under which circumstances deaths happen.

However, making use of this information is challenging. First, the summaries are plain natural language text which we need to process. Second, the bulk of reports makes processing of the summaries by humans rather difficult. A person would have to read or process more than 76,900 texts. If each summary takes a minute to read and file or process in any way, it would amount to approximately 1282 hours of work (or 160 work days if a work day consists of 8 hours).

There are three possible strategies to deal with such data: either the reports are processed by crowdsourcing them to a high number of people. Or, if there is an a priori defined category system, one may classify the reports into these categories with a supervised approach. Both strategies were not feasible. Hence, we used a technique that at the same time generates a category system and provides meta-information, which can then be used for aggregating reports with similar content.

### 3. Method.

3.1. *Using topic models to build splitting variables from report summaries.* There exist several approaches for extracting and handling textual information from documents. One strategy is to cluster the documents by matching them against predefined queries of terms, with the drawback that this might be inaccurate due to polysemy (multiple meanings) and synonymy of single terms. Latent Semantic Indexing (LSI) [Deerwester et al. (1990)] overcomes this by performing a singular value decomposition and thus mapping terms and documents into a latent semantic space. LSI provides more robust indicators of meaning than simple clustering but lacks in terms of a solid probabilistic foundation. This is solved by Hofmann (1999) and his seminal work on probabilistic LSI (pLSI). In pLSI, each word in a document is modeled as a sample from a mixture model specified via multinomial random variables. One drawback of pLSI, however, is that it provides no probabilistic structure at the level of documents. Blei, Jordan and Ng (2003) fill this gap by the specification of Latent Dirichlet Allocation (LDA).

LDA is a powerful document generative hierarchical model for clustering words into topics and documents into mixtures of topics. In LDA the topics are assumed to be uncorrelated [but see Blei and Lafferty (2007), for a version with correlated topics]. Assuming that the similarity of the circumstances between reports is reflected in the words contained in the respective summaries, we can use LDA to assign reports based on their summaries to a number of topics lower than the number of documents. Hence, in this fashion we use the allocation of each report to (one or more) latent topic(s) as a task of complexity reduction or as a preprocessing step.

According to Blei and Lafferty (2009), topics are automatically discovered from the original texts and no a priori information about the existence of a certain theme is required. This means LDA generates the category system by itself. Only the number of topics for the whole set of documents has to be specified. The resulting topics are shared across the whole set of documents. Please note that in general the topic distribution of each report does only include nonzero probabilities.

Regarding the appropriateness of topic models for such a task, Chang et al. (2009) presented results of a comparison of topic models with human classification. They concluded that “humans are able to appreciate the semantic coherence of topics and can associate the same documents with a topic that topic model does” [Chang et al. (2009), page 8]. Along similar lines, Griffiths and Steyvers [(2004), page 5228] note that “the extracted topics capture meaningful structure in the data, consistent with the class designations provided by the authors.”

3.1.1. *The report generative LDA model.* Following Blei and Lafferty (2009) and Blei (2012), LDA specifies the report generating process as a probabilistic model, in which each report is a mixture of a set of topics and each word in a report is chosen from the selected topic specific word distribution.

More formally, let  $q$  denote the size of a vocabulary (unique words within the considered corpus of reports) and let  $s$  be the number of topics  $\beta_t, t = 1, \dots, s$ . Each topic  $\beta_t$  is a  $q$ -dimensional symmetric Dirichlet distribution over the vocabulary with scalar parameter  $\eta$ . The only observed variables are words  $\mathbf{w}_{1:n}$ , where  $n$  denotes the number of reports and  $w_{d,m} \in \{1, \dots, q\}$  denotes the  $m$ th word of document  $d$ . The reports  $d, d = 1, \dots, n$ , are sequences of those words of varying lengths  $q_d$ . Each report  $d$  is assigned to topics with the assignments denoted by  $z_d$  and the topic assignment of each of its words  $w_{d,m}$  is denoted by  $z_{d,m}$ . Each report is seen as a mixture of topics and, hence, it has a vector of topic proportions denoted by  $\pi_d$ , with  $\pi_{d,t}$  denoting the proportion of topic  $t$  in report  $d$ . The distribution of  $\pi_d$  is an  $s$ -dimensional symmetric Dirichlet distribution with scalar parameter  $\kappa$ . Hence, the generative model for LDA is

$$(3.1) \quad P(\mathbf{w}_{1:n}, \beta_{1:s}, \pi_{1:n}, \mathbf{z}_{1:n} | \eta, \kappa) = \prod_{t=1}^s P(\beta_t | \eta) \prod_{d=1}^n \left[ P(\pi_d | \kappa) \left( \prod_{m=1}^{q_d} P(z_{d,m} | \pi_d) P(w_{d,m} | \beta_{1:s}, z_{d,m}) \right) \right],$$

where the conditional distributions of the topic assignments and the words are assumed to be categorical (multinomial with a single trial), that is,  $z_{d,m} \sim \text{Categorical}_s(\pi_d)$  and  $w_{d,m} \sim \text{Categorical}_q(\beta_{z_{d,m}})$ . For estimation of the model we employed the variational EM-Algorithm, which has the effect that  $\eta$  can remain unspecified [see, e.g., Grün and Hornik (2011)]. Since we use LDA to generate topics and assign each document to one of them, we need the posterior distribution of the latent topics, the topic assignment and the topic proportions given the documents,

$$(3.2) \quad P(\beta_{1:s}, \pi_{1:n}, \mathbf{z}_{1:n} | \mathbf{w}_{1:n}, \eta, \kappa) = \frac{P(\mathbf{w}_{1:n}, \beta_{1:s}, \pi_{1:n}, \mathbf{z}_{1:n})}{P(\mathbf{w}_{1:n})}$$

and the conditional expectations  $\hat{\beta}_{t,u} = E(\beta_{t,u} | \mathbf{w}_{1:n})$ ,  $\hat{\pi}_{d,t} = E(\pi_{d,t} | \mathbf{w}_{1:n})$  as well as  $\hat{z}_{d,t} = E(Z_d = t | \mathbf{w}_{1:n})$  with  $u = 1, \dots, q$ .

We follow suggestions in the pertinent literature [see Blei, Jordan and Ng (2003), Steyvers et al. (2004), Titov and McDonald (2008)] and omit stop words from the reports. Additionally, we use a stemmer to canonicalize different inflected forms to their base form (e.g., friends to friend). We then specify an a priori number of 100 latent topics to be estimated from the stop word free corpus of stemmed words. In addition, we set the parameter  $\kappa$  of the symmetric Dirichlet distribution of the topic proportions to a very small value (0.001) in order to ensure that the estimated topic distribution for each document will assign a probability of nearly one to a single topic and very small probabilities to all other topics. This makes it possible to switch from soft to hard assignments without substantial loss of information. The resulting dummy variables that encode whether a document belongs to a topic or not then serve as split candidate variables for subsequent analysis of the fatality numbers.

3.2. *Recursive partitioning of negative binomial distributions.* Our target variable is the number of fatalities per report  $Y_d$  ( $d = 1, \dots, n$ ), with realizations  $y_d$ . We use model trees with a prespecified node model to segment the data. This allows to incorporate information from  $p$  split candidate variables  $\mathbf{x}_d = (x_{1d}, \dots, x_{pd})^T$  for segmentation. Note that we model the fatalities locally in each segment and identify the segments based on statistical inference for the node models. This idea has objectives similar to model-based clustering. We choose recursive partitioning rather than mixture models because trees (i) expect all variables to interact with each other, (ii) automatically detect interactions, (iii) yield parsimonious interaction patterns, (iv) conduct variable selection due to the greedy forward search and (v) do not need the number of segments to be specified a priori.

More formally, the conditional distribution of  $Y$ ,  $D(Y|\cdot)$  is modeled as a partition function  $f$  depending on the state of  $p$  splitting vectors (variables),  $\mathbf{x} = (x_1, \dots, x_p)$ , that is,

$$(3.3) \quad D(Y|\mathbf{x}) = D(Y|f(x_1, \dots, x_p)),$$

where the function  $f$  partitions the overall splitting variable space  $\mathcal{X}$  into a set of  $r$  disjoint segments  $R_1, \dots, R_r$  such that  $\mathcal{X} = \bigcup_{k=1}^r R_k$  [Hothorn, Hornik and Zeileis (2006)]. In each segment  $R_k$ , a local model for the conditional distribution is fitted.

Our model for the conditional distribution  $D(Y|\mathbf{x})$  within each segment  $R_k$ ,  $k = 1, \dots, r$ , is a negative binomial distribution with mean  $\mu_k$  and shape parameter  $\theta_k$ , that is, having the probability mass function

$$(3.4) \quad P(Y = y|k; \mu_k, \theta_k) = \frac{\Gamma(y + \theta_k)}{\Gamma(\theta_k)y!} \left( \frac{\mu_k}{\mu_k + \theta_k} \right)^y \left( \frac{\theta_k}{\mu_k + \theta_k} \right)^{\theta_k}$$

with  $y \in \{0, 1, 2, \dots\}$ , and  $\Gamma(\cdot)$  denoting the gamma function. Mean and variance of  $Y$  for each segment  $R_k$  are given by [Lawless (1987)]

$$(3.5) \quad E(Y) = \mu_k, \quad \text{Var}(Y) = \mu_k + \mu_k^2 \theta_k^{-1}$$

and the segment size by  $n_k$ . Please note that the above formulation pays dues to interpreting the negative binomial as a gamma mixture of Poisson distributions [Aitkin et al. (2009)] and thus essentially being a Poisson model that can account for extra variation. It can be seen as a two-stage model for the discrete response  $Y$  in each segment  $R_k$  [cf. Venables and Ripley (2002)],

$$(3.6) \quad Y|V \sim \text{Poisson}(\mu_k V), \quad \theta_k V \sim \text{Gamma}(\theta_k).$$

Here  $V$  is an unobserved random variable having a gamma distribution with mean 1 and variance  $1/\theta_k$ . However, the marginal mean–variance identities for  $Y$  in (3.5) hold whenever  $V$  is a positive-valued random variable with mean 1 and variance  $\theta_k^{-1}$  and  $V$  need not necessarily be gamma distributed [Lawless (1987)]. Using the negative binomial distribution has the advantage over a Poisson model

to account for extra variation and over Quasi-Poisson to integrate nicely into a maximum likelihood framework [see Venables and Ripley (2002)]. In principle, the other count data models might also be used as the node model. In fact, a Quasi-Poisson model tree approach for modeling overdispersed count data has been proposed by Choi, Ahn and Chen (2005). Their rationale is similar to ours, but we use negative binomial distributions to account for overdispersion and a different tree algorithm that is unbiased in variable selection. The last point is very important for the correct interpretation of the tree structure [Kim and Loh (2001), Loh (2002), Loh and Shih (1997)] and depends on the splitting procedure [Loh (2009)].

3.2.1. *Estimation.* For simultaneous estimation of the segmentation and the node model parameters, we employ the model-based recursive partitioning framework of Zeileis, Hothorn and Hornik (2008). Hereby we consider an intercept-only model (i.e., there are no explanatory variables in the node model) estimated from a negative binomial likelihood which is then recursively partitioned based on the state of the split variables. For GLM-type models such as the negative binomial model, the algorithm is described in detail in Rusch and Zeileis (2013). This algorithm ensures that split variable selection is practically unbiased.

As tuning parameters for the tree algorithm we have the global significance level  $\alpha$  of the generalized M-fluctuation tests [Zeileis and Hornik (2007)] used for split variable selection and the minimum number of observations per node. Setting the former to low values can be regarded as pre-pruning to avoid overfit. As suggested for this procedure [Zeileis, Hothorn and Hornik (2008)], we let qualitative considerations guide our choice of tuning parameters. For this data set, significance levels of around 0.01 or higher might lead to spuriously significant results due to sample size, hence, we chose a low significance level of  $1 \times 10^{-4}$ . Additionally, we wanted to have at least 0.4% of the overall observations in a segment. Both choices were made to reduce fragmentation of the tree and to get a number of segments somewhere between 10 and 20.

Eventually we get a classification of all observations into a set of segments  $\mathcal{R} = \{R_1, \dots, R_r\}$ . The negative binomial distributions in these segments are characterized by the parameter estimates  $\hat{\mu}_k$  and  $\hat{\theta}_k, k = 1, \dots, r$ , and the estimated overall tree model by  $\hat{\boldsymbol{\vartheta}} = ((\hat{\mu}_1, \hat{\theta}_1)^T, \dots, (\hat{\mu}_r, \hat{\theta}_r)^T)$ .

3.2.2. *Interpretation of the models.* Basically, interpretation happens on two levels: first, the level of the individual segments for which we get the estimated mean number of fatalities as well as the associated standard deviation. These fatality rates identify which segments come along with a higher or lower average death toll. Second, the level of the splitting variables that define the segments. Here conclusions can be drawn about the specific circumstances that give rise to the segments and hence to the different fatality rates. In the case of topics as splitting variables, we only look at which topics are selected for splitting and interpret them *ex post* based on their most frequent words. Hence, topics are used only for

splitting without any further interpretation of or prior hypothesis about the underlying topic model. For readability we assign a unique name to each topic, but it should be kept in mind that those names are somewhat arbitrary. Since they are derived solely from the ten most frequent words as well as from looking at a random sample of assigned report summaries, they are necessarily neither exhaustive in their denotative and connotative meaning nor can they capture the circumstantial complexity of all assigned reports.

**4. Results and discussion.** In our analysis the response was the overall fatality number (sum of fatalities of civilians, the ACF, of coalition troops and of Afghan police and soldiers). Detailed analyses for all groups separately can be found in [Rusch et al. \(2011\)](#).

Along the lines of the methodological procedure described above and to understand the fatality numbers associated with different circumstances, we first need the split information, that is, which topics or further variables have been selected as splitting variables as well as where the split occurred. Second, we need the estimated parameters of the segment-specific model, that is, mean and shape. Accordingly, the split information is presented in [Figure 3](#) and the estimated node model parameters in [Table 2](#).

Regarding splits in the tree based on estimated latent topics, a presentation of their ten most frequent keywords and how many reports were assigned to them can be found in [Table 3](#) in [Appendix A](#) along with the absolute word frequency as a measure of word importance. For instance, the report summary from [Section 2](#) belongs to Topic 61, “Suicide and IED Bombing.” In [Table 3](#) the ten most frequent words of this (and other tree topics) are displayed, with “suicid” having occurred 520 times. Additionally, we can see in the first row of [Table 3](#) (`numberDOC`) that overall 378 incidents were assigned to this topic.

In [Figure 3](#) we visualize the negative binomial distribution in each segment by a parsimonious plot of the magnitudes of the mean and the standard deviation. The vertical line in each panel marks the location of the mean, the horizontal line shows the distance between zero and one theoretical standard deviation [cf. [Friendly \(2001\)](#)]. The height of the vertical line is the deviance divided by the degrees of freedom and indicates fit of the intercept-only model in the node. A smaller height means less dispersion and thus better fit (see also [Supplement B \[Rusch et al. \(2013b\)\]](#)).

We labeled the segments  $k = 1, \dots, r$  in an increasing order from right to left as they are displayed in the plot. This is of course arbitrary and should not imply a natural ordering of the  $k$  segments. Each segment  $R_k$  is associated with a local negative binomial distribution with parameter estimates  $\hat{\mu}_k$  and  $\hat{\theta}_k$ . For each segment, [Table 2](#) lists the segment number, parameter estimates and standard errors, degrees of freedom ( $n_k - 1$ ), deviance, the maximum number of fatalities and the percentage of incidents with no fatalities.

In what follows we discuss the results for the most interesting segments in more detail.

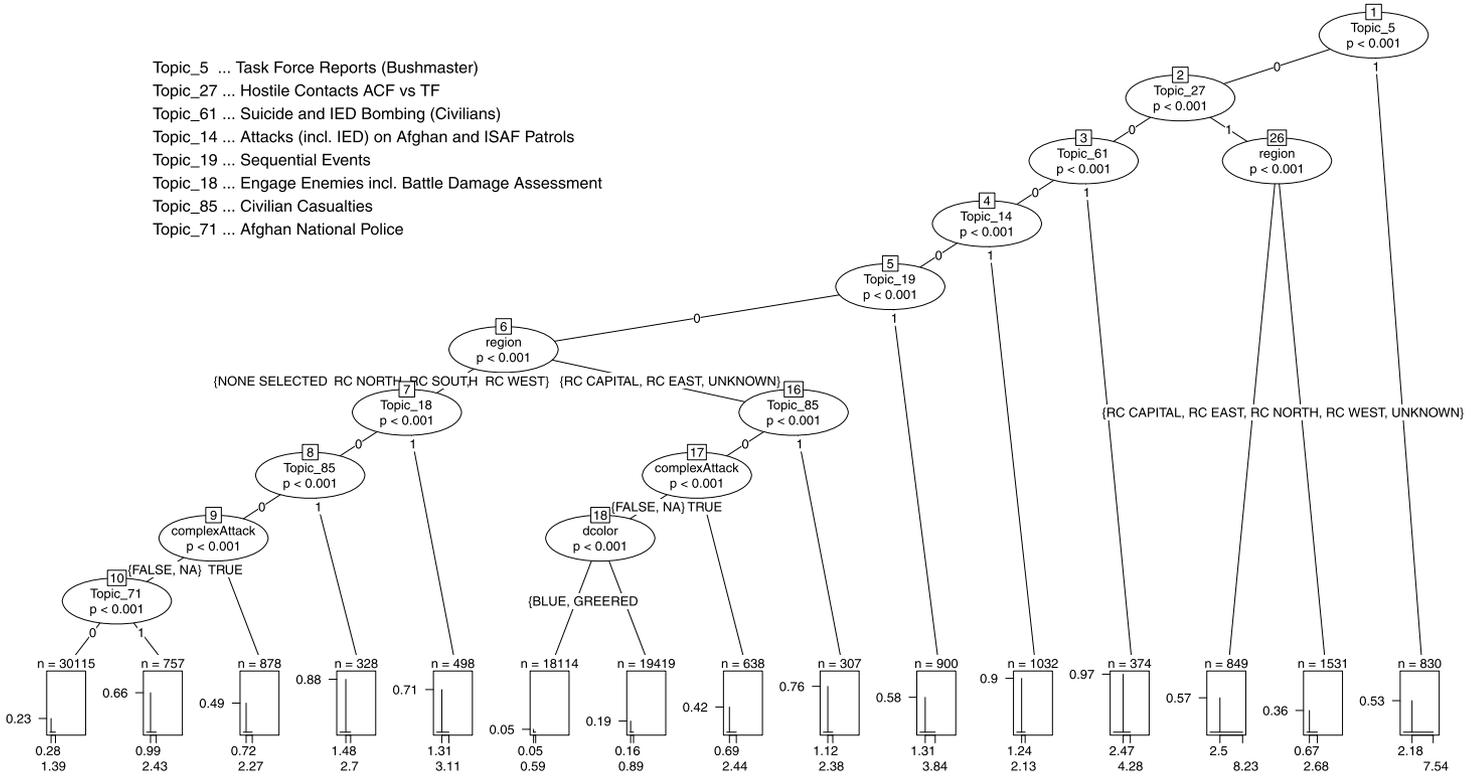


FIG. 3. The negative binomial model tree for the combined fatalities. In the segments the vertical line marks the mean, the horizontal line the length between zero and one standard deviation and the height of the vertical line is the deviance divided by the degrees of freedom (we included a larger version of this plot in Supplement A [Rusch et al. (2013a)]).

TABLE 2

Segment-wise statistics for all fatalities combined. The first column refers to the segment. For each segment we listed the logarithm of the estimated mean  $\log(\hat{\mu}_k)$ , its standard error  $\text{se}(\log(\hat{\mu}_k))$ , the estimated shape parameter  $\hat{\theta}_k$  and its standard error  $\text{se}(\hat{\theta}_k)$ , the degrees of freedom ( $df_k = n_k - 1$ ), the residual deviance (*dev*), the highest number of fatalities reported (*max*) and the percentage of reports with zero fatalities (*%zero*)

| Segment  | $\log(\hat{\mu}_k)$ | $\text{se}(\log(\hat{\mu}_k))$ | $\hat{\theta}_k$ | $\text{se}(\hat{\theta}_k)$ | $df_k$ | <i>dev</i> | <i>max</i> | <i>%zero</i> |
|----------|---------------------|--------------------------------|------------------|-----------------------------|--------|------------|------------|--------------|
| $R_1$    | 0.779               | 0.120                          | 0.089            | 0.007                       | 829    | 436.36     | 101        | 75.4         |
| $R_2$    | -0.399              | 0.102                          | 0.069            | 0.006                       | 1530   | 554.37     | 68         | 84.8         |
| $R_3$    | 0.917               | 0.113                          | 0.096            | 0.008                       | 848    | 486.90     | 186        | 72.4         |
| $R_4$    | 0.904               | 0.090                          | 0.386            | 0.038                       | 373    | 361.19     | 36         | 42.8         |
| $R_5$    | 0.215               | 0.053                          | 0.468            | 0.037                       | 1031   | 926.77     | 31         | 53.8         |
| $R_6$    | 0.269               | 0.098                          | 0.128            | 0.011                       | 899    | 523.48     | 70         | 73.1         |
| $R_7$    | 0.114               | 0.121                          | 0.275            | 0.039                       | 306    | 234.08     | 43         | 63.2         |
| $R_8$    | -0.376              | 0.146                          | 0.090            | 0.011                       | 637    | 267.76     | 25         | 82.3         |
| $R_9$    | -1.804              | 0.039                          | 0.043            | 0.002                       | 19,418 | 3604.80    | 28         | 93.4         |
| $R_{10}$ | -2.979              | 0.086                          | 0.009            | 0.001                       | 18,113 | 860.49     | 67         | 98.3         |
| $R_{11}$ | 0.269               | 0.106                          | 0.205            | 0.022                       | 497    | 353.50     | 56         | 66.3         |
| $R_{12}$ | 0.389               | 0.101                          | 0.373            | 0.046                       | 327    | 288.75     | 35         | 52.7         |
| $R_{13}$ | -0.329              | 0.106                          | 0.117            | 0.012                       | 877    | 425.75     | 35         | 79.3         |
| $R_{14}$ | -0.011              | 0.089                          | 0.199            | 0.019                       | 756    | 497.98     | 21         | 70.2         |
| $R_{15}$ | -1.282              | 0.029                          | 0.047            | 0.001                       | 30,114 | 6884       | 80         | 91.3         |

4.1. *Fatalities in the war logs.* For all fatalities combined, we find  $r = 15$  segments (with a global significance level for the fluctuation tests of  $\alpha = 1 \times 10^{-4}$  and a minimum number of observations in each segment of 300). The resulting tree is depicted in Figure 3.

The tree for the overall number of fatalities is dominated by fatalities of the ACF and of the civilian population. The tree itself is largely a combination of the trees for ACF and civilian fatalities alone [see Rusch et al. (2011)]. Our presentation will therefore mainly focus on ACF fatalities and civilian deaths, since those groups account for the highest number of deaths. Fatalities of allied forces and the troops of the host nation play a minor role for the overall number of deaths due to the comparatively small number of those fatalities (especially of allied forces) and the high congruency of civilian deaths and deaths of host nation troops.<sup>3</sup>

<sup>3</sup>For what follows, it should be noted that the entries in the database can be prone to data entry errors, mainly misclassification of fatalities to their respective group. For instance, the Kunduz air strike incident on 03-Mar-2009 lists 56 fatalities. All fatalities are stated to be “ACF fighters” in the war log. In the media, however, the killed people were identified as being civilians [see [guardian.co.uk](http://guardian.co.uk) (2010)] who were invited by the Taliban to take fuel from stolen fuel trucks [see [Amnesty International](http://Amnesty International) (2009)]. An allied air strike against the fuel trucks killed those 56 civilians. This should be kept in mind, although generally there is a high congruency between the data in the WikiLeaks war log and other independent data sets [Bohannon (2011)].

The first three segments are dominated by reports listing high numbers of fatalities of the ACF. These reports belong either to “Task Force Reports (Bushmaster)” or are associated with incidents attributable to “Hostile Contacts ACF vs TF” in the South and elsewhere.

The first segment consists of  $n_1 = 830$  incidents, with a maximum number of deaths of 101. 75.4% of the documents reported no fatalities. The average fatality number per report for this segment was  $\hat{\mu}_1 = 2.18$  (2.1 for ACF alone). The 101 ACF deaths that mark the maximum death toll in this segment is the third highest death number in the whole war diary, as is the mean fatality rate. All in all, 1808 deaths are reported in this segment, 1712 of those are categorized as ACF. This segment is characterized by reports that belong to Topic 5 “Task Force Reports (Bushmaster).” Table 3 displays the most frequent words in the summaries of this and subsequent topics along with their frequencies. For Topic 5 they were “task force,” “fire,” “close,” “track,” “insurgencies,” “bushmaster” and “isaf.” Inspection of report summaries from this topic suggests that this segment refers to reports by US task forces (TF) with a focus on actions of task force unit “Bushmaster.” TF “Bushmaster” is a task force consisting of Afghans and American green beret soldiers, the latter being a synonym for the United States Army Special Forces. According to Wikipedia, they have “six primary missions: unconventional warfare, foreign internal defense, special reconnaissance, direct action, hostage rescue, and counter-terrorism. The first two emphasize language, cultural, and training skills in working with foreign troops. Other duties include combat search and rescue (CSAR), security assistance, peacekeeping, humanitarian assistance, humanitarian de-mining, counter-proliferation, psychological operations, manhunts, and counter-drug operations” [Wikipedia (2011)]. The topic mainly describes events or fights connected with this and other TF, including detention of individuals, fights and espionage.

The next two segments are governed by Topic 27 “Hostile Contacts ACF vs TF” and differ in terms of the region they took place. They describe incidents where task forces or ground troops had enemy contact in fire fights taking place (individual combat with small arms, see Table 3). Excluded from this topic are reports from Topic 5. Incidents assigned to this topic are further split according to the region where the events took place. The right branch in Figure 3 contains events around Kabul (RC CAPITAL), RC EAST, RC WEST, RC NORTH and UNKNOWN regions, as collected in segment  $R_2$  which might be called “Hostile Contact ACF vs TF (not in the South).” These are associated with a death rate of  $\hat{\mu}_2 = 0.671$  (0.6 for ACF alone). Of these 1531 incidents the maximum number of fatalities is 68 and 84.8% reported no fatalities.

Of the reports belonging to Topic 27 “Hostile Contact ACF vs TF,” the 849 events that happened in the South of Afghanistan (mainly provinces Kandahar and Helmand, RC SOUTH) show a much higher estimated fatality rate of  $\hat{\mu}_3 = 2.501$  (2.4 for the ACF alone). This is the highest estimated death rate of any segment. It can be explained by the South, especially the province of Kandahar, being Taliban heartland and their stronghold. It is therefore heavily attacked by

coalition troops [see O’Loughlin et al. (2010)]. This result of higher death rates for incidents happening in the South is recurrent for all groups of fatalities [see Rusch et al. (2011)]. The segment “Hostile Contact ACF vs TF (South)” contains, among others, events that took place during Canadian-led “Operation Medusa,” which began on September 2, 2006 and lasted until September 17 [see Wikipedia (2010)]. Reports in this segment ( $R_3$ ) have a maximum number of fatalities of 186 on September 9, 2006. This report (its incident being part of “Operation Medusa”) notes 181 killed ACF fighters, one killed coalition force soldier and four killed Afghan soldiers 10 km southwest of Patrol Base Wilson, in Kandahar province’s volatile Zhari district. This is the highest number of killed ACF fighters (or overall death) within a single war log entry in the whole data set. Moreover, segment  $R_3$  is generally the segment with the highest ACF fatalities. Still, for 72.4% of the documents in this segment no fatalities are reported.

The next three segments we discuss consist of incidents that are characterized by a high death toll of the civilian population mainly resulting from actions of the ACF.

First, there is Topic 61 “Suicide and IED Bombing” with corresponding segment  $R_4$ . It describes incidents that were related to suicide bombing attacks or other attacks with improvised explosive devices (IED) such as cars (cf. Table 3). For example, one report assigned to Topic 61 and dated with 18-Feb-2008 reports 30 killed civilians due to a suicide bomb attack near Kandahar. It also includes reports where explosives were found or seized. The segment’s  $n_4 = 374$  reports list fatalities in 57.2% of the cases, which makes it the only segment with a median death number higher than 0. The maximum number of killed people is 36. Accordingly, the estimated mean death rate for this segment is  $\hat{\mu}_4 = 2.471$  (1.12 for civilians alone, the second highest civilian fatality rate). It is the second highest overall death rate per incident, closely matching the results from  $R_3$ . However, in  $R_4$  “Suicide and IED Bombing” fatalities are mostly civilians or Afghan police forces, whereas deaths in  $R_3$  “Hostile Contacts ACF vs TF (South)” are mostly ACF fighters. In  $R_4$  we observe 924 deaths, of which 420 are civilian, followed by 246 killed afghan soldiers and 233 killed ACF fighters.

The next segment is  $R_7$  “Civilian Casualties (East, Capital and unknown regions)” with an overall average number of fatalities of  $\hat{\mu}_7 = 1.12$ . These are those  $n_7 = 307$  incidents in the East, the capital or unknown region associated with Topic 85 “Civilian Casualties.” In Table 3 we see the clear context of civilian fatalities of this topic. Out of the ten most frequent terms of this topic, six are synonyms, respectively, acronyms of civilians. These are as follows: “ln” (local national), “local(s),” “civilian,” “lns” (local nationals), “child,” “nationals.” The other four terms suggest a clear connection to casualties, namely, “wound,” “injur” (injury), “kill,” “hospit” (hospital). The maximum number of fatalities in this segment is 43 and there are 63.2% of reports that list no fatality at all.

Segment  $R_{12}$  (governed by events from Topic 85 “Civilian Casualties” happening in the South, North, West or in a nonspecified region) has an estimated mean of

$\hat{\mu}_{12} = 1.476$ . The percentage of reports without killings is 52.7% and the highest death toll is 35. The governing topic, Topic 85, appeared before as the governing topic of  $R_7$ . Therefore,  $R_{12}$  and  $R_7$  are corresponding topic-wise and only differ in terms of their location. It is interesting to see that  $R_{12}$  has a higher fatality number per incident, most probably due to events in the south. Incidents in Kabul and the East ( $R_7$ ) are associated with lower death numbers and a higher percentage of reports with zero deaths. However, the report with the highest fatality number for this topic is part of  $R_7$ , describing an attack on the Indian embassy in Kabul where 42 civilians and one Taliban were killed.

When looking at civilian fatalities alone, incidents from Topic 85 “Civilian Casualties” have the overall highest observed civilian death toll for actions of the ACF, either against civilians or where civilians are “collateral damage” (on average 1.7 deaths per incident). Hence, incidents from this topic as well as incidents in Topic 61 “Suicide and IED Bombing” have in common that the attacks were overwhelmingly carried out by the ACF and were directed at places where there is a high number of the civilian population present, such as buses, bazars or markets. In contrast, for incidents which refer to actions of ISAF troops also belonging to Topic 85 “Civilian Casualties,” we have about 25% of the former rate (0.41 deaths per incident, the fourth highest overall rate for civilians). Thus, ACF action is associated with a fourfold increase in expected civilian fatalities for reports belonging to this topic. It is a clear and consistent finding that actions of the ACF come along with a higher civilian death toll than actions of the allied forces. Generally, when analyzing civilian fatalities alone, most resulting segments with high civilian fatality rates have in common that they are connected to attacks by the ACF often with improvised explosive devices [see also Bohannon (2011)].

The last segment we discuss is governed by Topic 14 “Attacks (incl. IED) on Afghan and ISAF patrols,” which gives rise to segment  $R_5$  with an average number of deaths per incident of  $\hat{\mu}_5 = 1.241$  (0.32 for the civilian population and 0.51 for Afghan troops). In total, we observe 1287 deaths in the  $n_5 = 1032$  reports (53.8% of which had no deaths reported) in this segment. It is somewhat hard to identify the governing topic with a unique theme like before, but inspecting a sample of report summaries indicates that this topic collects reports which describe explosions of IED or smaller fights or incidents following attacks by the ACF mainly with Afghan and some ISAF forces that were patrolling, resulting in battle damage assessment (bda) and medical evacuation. Most victims in this segment are therefore Afghan soldiers (529), but we also observe 326, 170 and 262 killed civilians, ACF and allied soldiers, respectively.

It should also be noted (and this finding is consistent throughout all the fatality groups) that segments containing by far the largest number of reports have on average relatively low death rates per incident and feature underdispersion. For all fatalities, these are segments  $R_{15}$ ,  $R_{10}$  and  $R_9$  with  $\hat{\mu}_{15} = 0.28$ ,  $\hat{\mu}_{10} = 0.05$  and  $\hat{\mu}_9 = 0.16$ . They contain 88.35% of all reports. Hence, most of the everyday happenings in this war come along with a low death toll. Only in the case of certain

events this number increases. This increase is mainly connected to either fights between allied forces and the Taliban and other ACF groups (leading to high ACF fatality numbers) or is characterized by attacks by the ACF who aim at or tolerate civilian casualties (leading to high civilian or Afghan troop fatality numbers).

**5. Model validation.** To keep in line with the objectives of our model tree approach, we validate the clustering structure and—locally for each cluster—the parametric model. Specifically, we (i) assess stability of the tree structure and reproducibility of the resulting segmentation and (ii) evaluate the fit of the local models. A detailed exposition of the validation results is available as [Supplement B \[Rusch et al. \(2013b\)\]](#).

*Stability of tree structure and segmentation.* We use resampling with replacement to generate data sets of  $5/6$  the size of the original data set. We fit model trees to the resampled data sets (tuning parameters modified to  $\alpha = 10^{-3}$  and a minimum number of observations of 250—due to the reduction in sample size). We use two resampling schemes: (i) regular resampling (RRS; i.e., drawing data sets of size  $5/6 \times n$  by random resampling with replacement) and (ii) stratified resampling (SRS; i.e., drawing from each segment  $R_k$  a proportion of  $5/6 \times n_k$  reports by random resampling with replacement). For each resampled data set, the fitted tree is then used to predict the segment and the fatality number for the reports not part of the set of resampled reports (the out-of-bag observations). Thus, we get segment assignments for all in-bag and out-of-bag reports. The procedure is repeated 200 times per resampling scheme.

We use a segment-wise version of the Jaccard index [[Jaccard \(1901\)](#)] as the measure of segment stability and report concordance. See [Supplement B](#) or [Hennig \(2007\)](#) for details. Possible alternative measures include “prediction strength” [[Tibshirani and Walther \(2005\)](#)]. Let  $T$  denote the original tree and  $T^{(b)}$  the tree fitted on bootstrap sample  $b$  with  $T$  having the segments  $R_k, k = 1, \dots, r$ , and  $T^{(b)}$  the segments  $R_l^{(b)}, l = 1, \dots, r^{(b)}$ . We denote the segment-wise Jaccard index for each resample  $b$  by  $\text{Jac}_{kl}^{(b)}$  with  $k = 1, \dots, r$  and  $l = 1, \dots, r^{(b)}$ . For each resample  $b$  and given segment  $R_k$  we calculate the segment-wise indices  $\text{Jac}_{kl}^{(b)}$  and assign the segment  $R_l^{(b)}, l : \arg \max_l \text{Jac}_{kl}^{(b)}$  to be the corresponding segment of  $R_k$ , that is, with concordance  $\text{Jac}_k^{*(b)} = \max_l \text{Jac}_{kl}^{(b)}$  (see [Supplement B](#) for details).

When investigating the corresponding tree segments, we find that pooled over the RRS and SRS scheme (the results do not differ much for each scheme, see [Figure 4](#) and the supplementary material [[Rusch et al. \(2013a, 2013b\)](#)]) there are 27.6% coinciding segments ( $\text{Jac}_k^{*(b)} = 1$ ) and 56.3% strongly corresponding segments ( $\text{Jac}_k^{*(b)} \geq 0.8$ ) over the 400 resamples.

This is more pronounced for the segments discussed in detail in [Section 4.1](#). Here we have 42.3% coinciding segments and 62.4% of the segments show strong

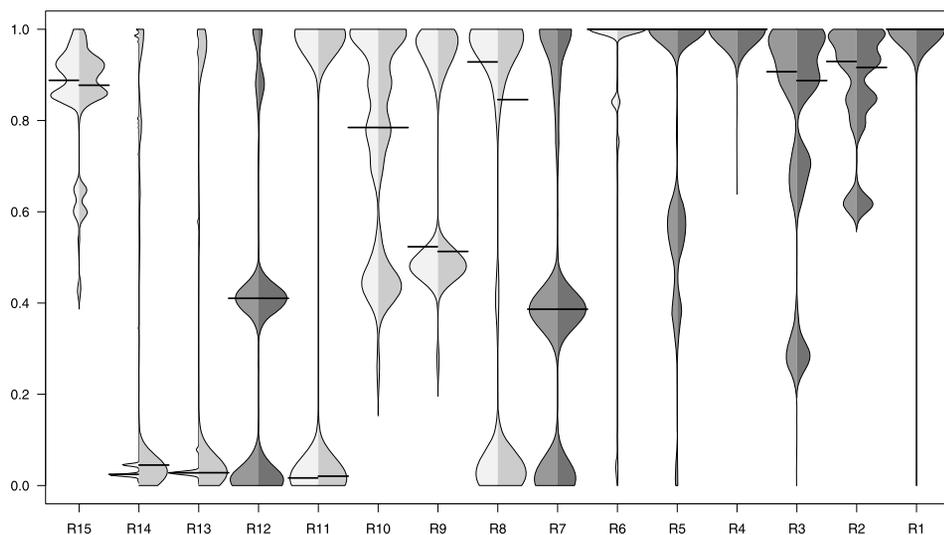


FIG. 4. Bean plots of the segment-wise Jaccard indices,  $\text{Jac}_k^{*(b)}$ , between original segments and the matched segments over the bootstrap samples  $b$  for all  $R_k$ ,  $k = 1, \dots, 15$ . Darker beans mark segments we described in detail in Section 4.1. The left part of each bean is a kernel density estimate for RRS (slightly lighter shaded) and the right-hand side for SRS (slightly darker shaded). The solid black lines are the medians.

correspondence. Note that the first five described segments,  $R_1$  through  $R_5$ , show even higher frequencies (56.2% coinciding and 79% strongly corresponding). Thus, the results can be considered to be stable with the exception of the segments associated with Topic 85 ( $R_7$  and  $R_{12}$ ), which have a percentage of 9.2% coinciding segments and 20.9% strongly corresponding segments.

Regarding stability of the individual segments, the distribution of the concordance measure  $\text{Jac}_k^{*(b)}$  for each segment  $R_k$  over the bootstrap samples is summarized with bean plots [Kampstra (2008)] in Figure 4. The solid black horizontal lines denote the medians. High stability (median  $\geq 0.79$ ) is given for 9 out of 15 segments:  $R_1$  through  $R_5$  (from Section 4.1) as well as  $R_6$ ,  $R_8$ ,  $R_{10}$  and  $R_{15}$ . For those, 50% of the corresponding segments show a concordance of at least 0.79. The mass of the Jaccard values is usually concentrated near the median, the exceptions being  $R_{10}$  and  $R_8$  and to a minor degree  $R_2$  and  $R_3$ . For certain segments variability is quite high, particularly for  $R_{10}$  and  $R_8$ . For the segments discussed in detail in Section 4.1 the stability is highest, with a median of 0.79 or higher in 5 of 7 segments. Low stability is found for segments  $R_{14}$ ,  $R_{13}$  and  $R_{11}$ . Also,  $R_{12}$  and  $R_7$  are not particularly stable.

*Segment-wise variability of fatality rates.* To evaluate stability of the local models, we investigate the variability of the estimates of the model parameters for each segment. We match a given segment  $R_k$  from  $T$  with a segment  $R_l^{(b)}$  from

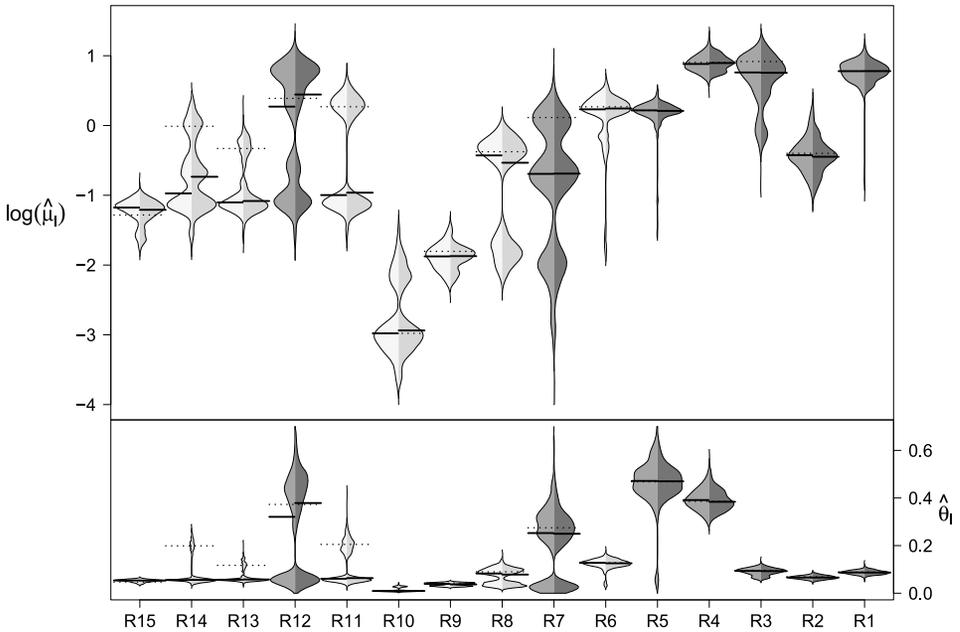


FIG. 5. Bean plots of the segment-wise estimated death toll parameter  $\log(\hat{\mu}_l)$  and shape parameter  $\hat{\theta}_l$  for the matched segments. The dotted horizontal lines indicate the values of the original tree (compare Table 2). Again, darker beans mark segments described in detail in the paper. The left part of each bean is for RRS (slightly lighter shaded) and the right-hand side for the SRS (slightly darker shaded).

$T^{(b)}$  based on the highest Jaccard index for each bootstrap sample as before. For each segment  $k$ , Figure 5 displays bean plots of the distributions of the parameter estimates  $\log(\hat{\mu}_l)$  and  $\hat{\theta}_l$  for the matched segments over all samples. The dotted horizontal lines indicate the parameter values estimated for the original tree. The results are in line with those presented before. We have ten stable segments of the original tree  $R_1$  through  $R_6$ ,  $R_8$  through  $R_{10}$  and  $R_{15}$ . Over the bootstrap samples, their median estimated parameter values in the segments turn out to lie close to the original  $\log(\hat{\mu}_k)$ . For most  $R_k$  the variability of  $\log(\hat{\mu}_l)$  over the bootstrap samples is rather small. Among them are five segments that we described in detail in Section 4.1, associated with the topics “Task Force Reports (Bushmaster),” “Hostile Contacts ACF vs TF,” “Suicide and IED Bombing” and “Attacks (incl. IED) on Afghan and ISAF patrols.” They are reproducible both in terms of the assigned reports and the parameters for the local models. We also have three unstable segments ( $R_{11}$ ,  $R_{14}$  and  $R_{13}$ ) and two low to moderately stable segments ( $R_{12}$  and  $R_7$ ). They are practically the same segments that turned out to be unstable in the previous section. These segments appear further down the tree hierarchy (see Figure 3) and arise from the branches after the split of node 6 based on region. Among them are the segments associated with Topic 85 “Civilian Casual-

ties” ( $R_7$  and  $R_{12}$ ). To have a more reliable description for these two segments, an analysis considering only the number of civilian fatalities might be better and can be found in [Rusch et al. \(2011\)](#).

*Appropriateness of the node model.* To judge the fit of the local models in the nodes, we report the deviance and the degrees of freedom in Table 2. As can be seen in detail in Section 2.1 of [Supplement B](#), the deviance values, their ratio to the degrees of freedom, the mean absolute prediction error and the residuals all point to a good fit of the segments-wise models (although for some segments we find substantially less variability as the model would predict). We further compared the fit of the negative binomial model to alternative count data models per segment. Each segment shows substantial overdispersion as compared to a Poisson model (see Section 2.2 in [Supplement B](#)). Inflation of zeros for a negative binomial model could not be found in any segment. In each segment the negative binomial model was the count data distribution with lowest AIC/BIC and highest likelihood (see Section 2.3 in [Supplement B](#)). We also checked for severe violations of the temporal independence assumption for residuals in each segment. We generally find no to small autocorrelation in the order the reports have been filed (see Section 2.4 in [Supplement B](#)), hence, the independence assumption appears to be an acceptable approximation.

**6. Conclusions.** Undoubtedly, innovations like the internet have changed the supply of potential data of interest. For science as well as journalism, it is unavoidable to gather, manage and process this bulk of information. Central to this is reading, interpreting and understanding text documents with the aid of automated procedures. The foreseeable increase of available written information, for example, in the world wide web, will even increase the need for such methods. At least partly, this has nourished data journalism and computational social science where complex data sets become the center of journalistic and scientific work. This paper illustrates how modern statistical procedures can provide aid in extracting relevant information from bulks of written text documents or from a database and how they may help in processing and structuring the information to facilitate interpretation of the data, as has been the primary goal of statistical modeling ever since.

Text mining tools and topic models were used to analyze written text from the WikiLeaks war diary automatically by assigning overarching themes to the single documents. This allowed to get a view on the data which is hard to obtain by manual processing and that may even discover connections between documents which may not be at all obvious. The assignment of topics to the single documents offered the opportunity to use those topics as splitting variables in further data analysis. One has to bear in mind, however, that the assignment of documents to topics is by far not absolute and that it can be difficult to interpret the meaning of latent topics, especially if they are to be named (as is often the case with unsupervised

techniques). At any rate, we saw that split candidate variables generated by preprocessing with LDA proved to be very important in the subsequent analysis, whereas the variables that were already available played a minor role. Hence, discarding the information stored in the report summaries would have led to completely different segmentation, description and interpretation.

Model-based trees were then used to find segments in the data as well as for providing an intuitive association of circumstances and fatalities. A representative local data model (here the negative binomial distribution) was used to relate the observations to the question at hand. Instead of simply calculating the arithmetic mean of the dependent variable, the underlying model takes a whole likelihood for overdispersed count data—suitable for the description of rare events—into account when estimating the segmentation, the mean fatality rate and the variance in each segment. Pre-pruning with an inferential splitting procedure led to a segmentation that proved to be rather stable in resampling experiments, especially with respect to the segments that we primarily focused on. The segment assignment of reports and the estimated parameter values were reproducible when applied to random subsets of all reports. The local models in the segments fit the data at hand well. The model tree based segmentation approach that we chose therefore offered reliable, additional insight into what the fatality rates for specific incidents look like, something that has not been done so far for this war.

This clearly illustrates the high potential that text mining procedures, on the one hand, and model-based recursive partitioning, on the other, have for a wide range of possible applications in social sciences [see, e.g., [Kopf, Augustin and Strobl \(2010\)](#)] as well as data journalism, especially if the data stem from a database or consist of both numerical variables and written text which has to be analyzed, for example, with data from online forums, social media or social networks.

Despite the insights our approach can provide, we see room for improving it in future research. First, we did not exploit all of the spatial and temporal information that is contained in the data set. While revising this paper, we became aware of the work by [Zammit-Mangion et al. \(2012\)](#) who made use of the temporal and spatial aspects. It might be interesting to combine their and our strategy by using their model as a node model and partition it based on the generated topic assignments. Second, instead of a two-step procedure, we started working on a generic model that includes both the preprocessing step as well as the step of fitting the count data model simultaneously.<sup>4</sup>

#### APPENDIX A: FREQUENT TERMS OF THE TOPICS

In [Table 3](#) a list of the ten most frequent terms for each topic as well as their occurrence for different fatality groups and the number of documents assigned to them can be found.

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<sup>4</sup>We thank an anonymous reviewer for this suggestion.

TABLE 3

The ten most frequent terms of the estimated latent topics and the number of documents assigned. A × denotes that this topic serves as a split variable for the mentioned subgroup as well. Numbers in brackets indicate the term frequencies in the assigned reports

|           | Topic 5         | Topic 14      | Topic 18      | Topic 19      | Topic 27       | Topic 61     | Topic 71         | Topic 85       |
|-----------|-----------------|---------------|---------------|---------------|----------------|--------------|------------------|----------------|
| numberDOC | 830             | 1035          | 508           | 900           | 2382           | 378          | 1288             | 638            |
| CIVILIAN  |                 | ×             |               |               |                | ×            | ×                | ×              |
| ACF       | ×               |               | ×             | ×             | ×              |              |                  |                |
| ISAF      |                 | ×             |               |               |                | ×            |                  |                |
| HOST      |                 | ×             |               |               |                | ×            | ×                |                |
|           | tf (1994)       | wia (2004)    | engag (1761)  | updat (4157)  | fire (3345)    | suicid (520) | anp (4132)       | ln (1595)      |
|           | bushmast (1570) | ie (1981)     | fire (1092)   | att (1742)    | tf (2979)      | bomber (470) | event (643)      | wound (799)    |
|           | fire (1314)     | cat (1376)    | damag (923)   | event (1331)  | enemi (2795)   | deton (377)  | attack (620)     | local (543)    |
|           | forc (990)      | bda (1045)    | bda (908)     | saf (1205)    | tic (2128)     | vest (294)   | close (603)      | kill (389)     |
|           | close (742)     | strike (1005) | mm (705)      | fire (1071)   | contact (1933) | attack (282) | ie (592)         | hospit (385)   |
|           | friend (737)    | kia (849)     | pid (667)     | aaf (955)     | element (1933) | explos (257) | wia (484)        | civilian (357) |
|           | isaf (703)      | isaf (837)    | compund (635) | pax (902)     | acm (1635)     | nds (222)    | cp (471)         | injur (280)    |
|           | insurg (659)    | medevac (777) | ground (613)  | contact (818) | receiv (1480)  | kill (195)   | isaf (466)       | child (239)    |
|           | track (593)     | vehicl (721)  | kill (576)    | vc (666)      | saf (1361)     | khowst (126) | qrf (294)        | nation (232)   |
|           | event (574)     | struck (590)  | ah (368)      | station (653) | arm (1148)     | svbi (112)   | checkpoint (263) | lms (216)      |

## APPENDIX B: COMPUTATIONAL DETAILS

All calculations have been carried out with the statistical software R 2.12.0-2.15.1 [R Development Core Team (2012)] on `cluster@WU` [FIRM (2011)]. Topic models were estimated with the extension package `topicmodels` 0.0-7 [Grün and Hornik (2011)]. Further packages used were `slam` 0.1-18 and `tm` 0.5-4.1. Recursive partitioning infrastructure was provided by the function `mob()` [Zeileis, Hothorn and Hornik (2008)] from the package `party` 0.9-99991. Further packages used were `strchange` 1.4-3. The negative binomial family model for `mob` can be found in the package `mobtools` 0.0-1 [Rusch et al. (2012)]. It uses `glm.nb()` in package `MASS` 7.3-7 [Venables and Ripley (2002)].

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## SUPPLEMENTARY MATERIAL

**Supplement A: Data, code and plot** (DOI: 10.1214/12-AOAS618SUPPA; .zip). A bundle containing the data sets, the code files and a high-resolution version of Figure 3.

**Supplement B: Model validation** (DOI: 10.1214/12-AOAS618SUPPB; .pdf). A detailed description of our validation steps and their results.

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